

Calculus Reference Sheet C: Introducing Definite Integrals

Limits			
$\lim_{x \rightarrow c} [f(x) \pm g(x)] = \lim_{x \rightarrow c} f(x) \pm \lim_{x \rightarrow c} g(x)$	$\lim_{x \rightarrow c} [f(x) \times g(x)] = \lim_{x \rightarrow c} f(x) \times \lim_{x \rightarrow c} g(x)$		
Derivatives			
Rules			
Constant	$\frac{d}{dx} [c] = 0$	Single variable	$\frac{d}{dx} [ax] = a$
Sum and difference	$\frac{d}{dx} [f(x) \pm g(x)] = f'(x) \pm g'(x)$	Power	$\frac{d}{dx} [x^n] = n \times x^{n-1}$ $\frac{d}{dx} [g(x)^n] = n(g(x))^{n-1} \times g'(x)$
Product	$\frac{d}{dx} [f(x) \times g(x)] = f(x) \times g'(x) + g(x) \times f'(x)$	Quotient	$\frac{\frac{d}{dx} [f(x)]}{\frac{d}{dx} [g(x)]} = \frac{g(x)f'(x) - f(x)g'(x)}{[g(x)]^2},$ $g'(x) \neq 0$
Chain	$f' \circ g(x) = f'(g(x)) = f'(g(x)) \times g'(x)$	Exponential	$\frac{d}{dx} [e^{g(x)}] = g'(x) \times e^{g(x)}$
Integrals			
Definite			
Definition	$\int_a^b f(x) dx = \lim_{n \rightarrow \infty} \sum_{i=1}^n f(x_i) \Delta x$		
Rules			
Constant	$\int_a^a f(x) dx = 0$	Single variable	$\int_a^b c dx = cx$
Sum and difference	$\int_a^b [f(x) \pm g(x)] = \int_a^b f(x) dx \pm \int_a^b g(x) dx$	Additive	$\int_b^a f(x) dx = - \int_a^b f(x) dx$
Power	$\int_a^b x^n dx = \frac{x^{n+1}}{n+1},$ $n \neq -1$	Exponential	$\int_a^b c^x dx = \frac{c^x}{\ln c}$